

1. Using the graph below, decide whether each statement is true or false. If false, give the correct answer.

a) $\lim_{x \rightarrow -1^+} f(x) = 1$

b) $\lim_{x \rightarrow 0^-} f(x) = 0$

c) $\lim_{x \rightarrow 0^+} f(x) = 1$

d) $\lim_{x \rightarrow 0^+} f(x) = \lim_{x \rightarrow 0^-} f(x)$

e) $\lim_{x \rightarrow 0} f(x)$ does not exist

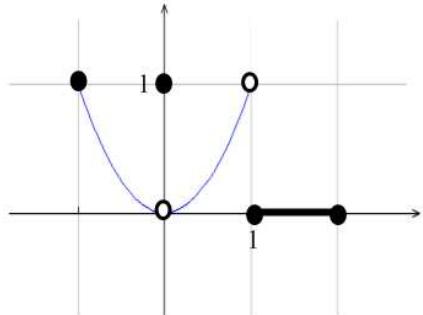
f) $\lim_{x \rightarrow 1^+} f(x) = 1$

g) $\lim_{x \rightarrow 1^-} f(x) = 1$

h) $\lim_{x \rightarrow 1} f(x) = 1$

i) $\lim_{x \rightarrow 2^-} f(x) = 2$

j) $f(1) = 1$



2. Determine each limit.

a) $\lim_{x \rightarrow 0^+} [[x]]$

b) $\lim_{x \rightarrow 0^-} [[x]]$

c) $\lim_{x \rightarrow 0} [[x]]$

d) $\lim_{x \rightarrow 0.1} [[x]]$

e) $\lim_{x \rightarrow 2^-} [[x]]$

f) $\lim_{x \rightarrow -3^+} [[x]]$

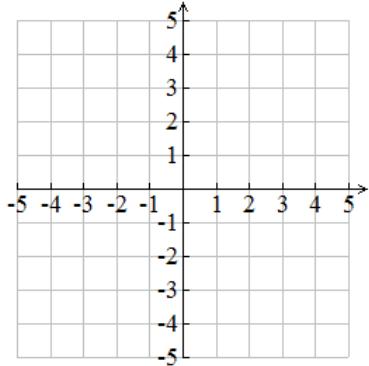
g) $\lim_{x \rightarrow 0^+} \frac{x}{|x|}$

h) $\lim_{x \rightarrow 0} \frac{x}{|x|}$

i) $\lim_{x \rightarrow 0} \frac{\sin x}{2x^2 - x}$

3. Sketch the graph of $f(x) = \begin{cases} 3-x, & x < 2 \\ \frac{x}{2} + 1, & x > 2 \end{cases}$. Then find the following.

a) $\lim_{x \rightarrow 2^-} f(x)$



b) $\lim_{x \rightarrow 2^+} f(x)$

c) $\lim_{x \rightarrow 2} f(x)$

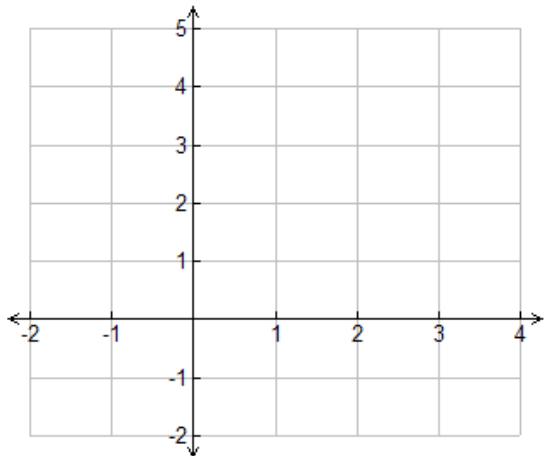
Sketch the graphs of the following functions. Then answer each question.

$$4. \quad g(x) = \begin{cases} 3-x, & x < 2 \\ \frac{x}{2}, & x > 2 \\ 2, & x = 2 \end{cases}$$

a) $\lim_{x \rightarrow 2^-} g(x)$

b) $\lim_{x \rightarrow 2^+} g(x)$

c) $\lim_{x \rightarrow 2} g(x)$



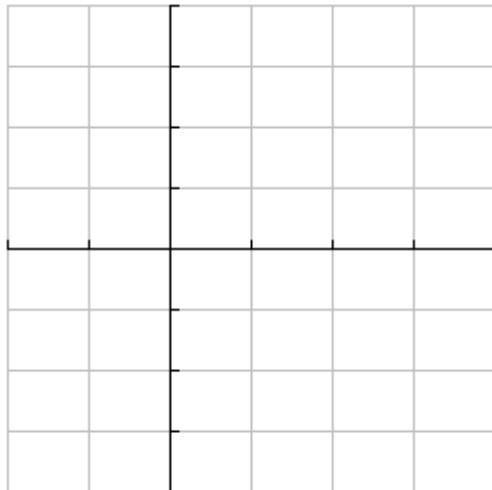
$$5. \quad f(x) = \begin{cases} \sin x, & x < 0 \\ 1 - \cos x, & 0 \leq x \leq \pi \\ \cos x, & x > \pi \end{cases}$$

a) $\lim_{x \rightarrow 0^-} f(x)$

b) $\lim_{x \rightarrow 0^+} f(x)$

c) $\lim_{x \rightarrow 0} f(x)$

d) $\lim_{x \rightarrow \pi} f(x)$



$$6. \quad f(x) = h(x) = \begin{cases} x, & x < 0 \\ x^2, & 0 < x \leq 2 \\ 8 - x, & x > 2 \end{cases}$$

a) $\lim_{x \rightarrow 0^-} h(x)$

b) $\lim_{x \rightarrow 0^+} h(x)$

c) $\lim_{x \rightarrow 0} h(x)$

d) $\lim_{x \rightarrow 2} h(x)$

